\$ubject: Theory of computation topic: NFA
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## Non-Deterministic Finite Automata-

In Non-Deterministic Finite Automata,

- For some current state and input symbol, there exists more than one next output states.
- A string is accepted only if there exists at least one transition path starting at initial state and ending at final state.


## Converting NFA to DFA-

The following steps are followed to convert a given NFA to a DFA-

## Step-01:

Let Q' be a new set of states of the DFA. Q' is null in the starting.
Let T' be a new transition table of the DFA.

## Step-02:

## Add start state of the NFA to Q'.

Add transitions of the start state to the transition table T'.
If start state makes transition to multiple states for some input alphabet, then treat those multiple states as a single state in the DFA. In NFA, if the transition of start state over some input alphabet is null, then perform the transition of start state over that input alphabet to a dead state in the DFA.

## Step-03:

If any new state is present in the transition table $T^{\prime}$,
Add the new state in Q'.
Add transitions of that state in the transition table T'.

## Step-04:

Keep repeating Step-03 until no new state is present in the transition table T'.

Finally, the transition table T' so obtained is the complete transition table of the required DFA.

## PRACTICE PROBLEMS <br> BASED_ON CONVERTING NFATO DFA:

## Problem-01:

Convert the following
Non-Deterministic Finite Automata (NFA) to Deterministic Finite Automata (DFA)-

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Convert the following Non-Deterministic Finite Automata (NFA) to Deterministic Finite Automata (DFA)-


## Solution-

Transition table for the given Non-Deterministic Finite Autamotn (NIEN) in

| State / Alphabet | a | b |
| :---: | :---: | :---: |
| $\rightarrow \mathbf{q} 0$ | q0 | q0, q1 |
| q1 | - | *q2 |
| *q2 | - | - |

## Step-01:

Let Q' be a new set of states of the Deterministic Finite Automata (DFA).

Let T' be a new transition table of the DFA.

## Step-02:

Add transitions of start state $\mathrm{q0} 0$ to the transition table $\mathrm{T}^{\text {'. }}$.

## Step-03:

New state present in state $Q^{\prime}$ is $\{q 0, q 1\}$.
Add transitions for set of states $\{q 0, q 1\}$ to the transition table T'

## Step-04:

New state present in state Q' is $\{q 0, q 1$, q2\}.

Add transitions for set of states $\{q 0, q 1$, q2\} to the transition table T '.

| State / Alphabet | $\mathbf{a}$ | $\mathbf{b}$ |
| :---: | :---: | :---: |
| $\rightarrow \mathbf{q 0}$ | q 0 | $\{q 0, \mathrm{q} 1\}$ |
| $\{q 0, q 1\}$ | q 0 | $\{q 0, \mathrm{q} 1, \mathrm{q} 2\}$ |
| $\{q 0, q 1, q 2\}$ | q 0 | $\{q 0, \mathrm{q} 1, \mathrm{q} 2\}$ |

## Step-05:

Finally, Transition table for Deterministic Finite Automata (DFA) is-
Since no new states are left to be added in the transition table T', so we stop.

States containing q2 as its component
are treated as final states of the DFA.

| State / Alphabet | $\mathbf{a}$ | $\mathbf{b}$ |
| :---: | :---: | :---: |
| $\rightarrow \mathbf{q 0}$ | q 0 | $\{q 0, \mathrm{q} 1\}$ |
| $\{q 0, q 1\}$ | q 0 | ${ }^{*}\{q 0, \mathrm{q} 1, \mathrm{q} 2\}$ |
| $*\{q 0, q 1, q 2\}$ | q 0 | ${ }^{*}\{q 0, \mathrm{q} 1, \mathrm{q} 2\}$ |



## Deterministic Finite Automata (DFA)

