

Subject:Discrete Mathematics

Topic:Laws of logic

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LAWS OF LOGIC



IDENTITY LAW

$$P \vee T \equiv T$$

$$P \wedge T \equiv P$$

$$P \vee F \equiv P$$

$$P \wedge F \equiv F$$

COMPLIMENT LAW

$$P \vee \sim P \equiv T$$

$$P \wedge \sim P \equiv F$$

$$\sim T \equiv F$$

$$\sim F \equiv T$$

INVOLUTION LAW

$$\sim(\sim P) \equiv P$$

DEMORGAN'S LAW

$$\sim(P \vee Q) \equiv \sim P \wedge \sim Q$$

$$\sim(P \wedge Q) \equiv \sim P \vee \sim Q$$

TRUTH TABLE FOR DEMORGAN'S LAW

p	q	$p \vee q$	$\sim p$	$\sim q$	$\sim(p \vee q)$	$\sim p \wedge \sim q$
T	T					
T	F					

CONDITIONAL STATEMENTS

If you listen my lecture carefully, then you will definitely understand this topic

Condition \rightarrow outcome


if you listen my lecture carefully: p

then you will definitely understand this topic: q

We can represent as “if p then q ”

$p \rightarrow q$ (implication of p)

CONDITIONAL STATEMENTS

A compound statement using the connective **if....then** is called a conditional statement or implication. A conditional statement is used as a guarantee for the conclusion to be true provided, condition is true. If p and q are two statements then compound statement if p then q denoted by $p \Rightarrow q$ is an implication and the connective ifthen is the conditional connective. The connective if....then is denoted by \Rightarrow / and can be read as

- p implies q
- p is sufficient for q
- p only if q
- q is necessary for p
- q is consequence of p

Note: p implies q and q implies p are completely different statements.

Truth Table for $p \Rightarrow q$

p	q	$p \Rightarrow q$
T	T	T
T	F	F
F	T	T
F	F	T

CONVERSE STATEMENT

The converse of a given conditional statement $p \Rightarrow q$ is a new statement found by interchanging the hypothesis p and the conclusion q of the given conditional statement.

If $p \Rightarrow q$ then converse of it is $q \Rightarrow p$

Eg: if i understood this topic, then i listened the lecture carefully.

if i understood this topic: q

then i listened the lecture carefully: p

TRUTH TABLE FOR $Q \Rightarrow P$

p	q	$q \Rightarrow p$
T	T	T
T	F	T
F	T	F
F	F	T