

Subject: Computer graphics

Topic : Rotation example problems

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Rotation

EXAMPLE PROBLEMS

PROBLEM

Given a triangle with corner coordinates $(0, 0)$, $(1, 0)$ and $(1, 1)$. Rotate the triangle by 90 degree anticlockwise direction and find out the new coordinates?

SOLUTION

- We rotate a polygon by rotating each vertex of it with the same rotation angle.

Given-

- Old corner coordinates of the triangle = A (0, 0), B(1, 0), C(1, 1)
- Rotation angle = $\theta = 90^\circ$

For Coordinates A(0, 0)

Let the new coordinates of corner A after rotation = $(X_{\text{new}}, Y_{\text{new}})$.

Applying the rotation equations, we have-

$$\begin{aligned} X_{\text{new}} &= X_{\text{old}} \times \cos\theta - Y_{\text{old}} \times \sin\theta \\ &= 0 \times \cos 90^\circ - 0 \times \sin 90^\circ \\ &= 0 \end{aligned}$$

$$\begin{aligned} Y_{\text{new}} &= X_{\text{old}} \times \sin\theta + Y_{\text{old}} \times \cos\theta \\ &= 0 \times \sin 90^\circ + 0 \times \cos 90^\circ \\ &= 0 \end{aligned}$$

Thus, New coordinates of corner A after rotation = (0, 0).

For Coordinates B(1, 0)

Let the new coordinates of corner B after rotation = $(X_{\text{new}}, Y_{\text{new}})$.

$$\begin{aligned} X_{\text{new}} &= X_{\text{old}} \times \cos\theta - Y_{\text{old}} \times \sin\theta \\ &= 1 \times \cos 90^\circ - 0 \times \sin 90^\circ \\ &= 0 \end{aligned}$$

$$\begin{aligned} Y_{\text{new}} &= X_{\text{old}} \times \sin\theta + Y_{\text{old}} \times \cos\theta \\ &= 1 \times \sin 90^\circ + 0 \times \cos 90^\circ \\ &= 1 + 0 \\ &= 1 \end{aligned}$$

Thus, New coordinates of corner B after rotation = $(0, 1)$.

For Coordinates C(1, 1)

Let the new coordinates of corner C after rotation = $(X_{\text{new}}, Y_{\text{new}})$.

$$X_{\text{new}}$$

$$= X_{\text{old}} \times \cos\theta - Y_{\text{old}} \times \sin\theta$$

$$= 1 \times \cos 90^\circ - 1 \times \sin 90^\circ$$

$$= 0 - 1$$

$$= -1$$

$$Y_{\text{new}}$$

$$= X_{\text{old}} \times \sin\theta + Y_{\text{old}} \times \cos\theta$$

$$= 1 \times \sin 90^\circ + 1 \times \cos 90^\circ$$

$$= 1 + 0$$

$$= 1$$

Thus, New coordinates of corner C after rotation = (-1, 1).

